

Applications to Butler-Volmer equation, Chapter 3

Practical numerical application :

$|\eta| > 0.1 \text{ V}$ Tafel:

Anodic current for +ve η ; $i = i_0 \exp\{(1 - \alpha) \eta F/RT\}$

Cathodic current for -ve η ; $i = i_0 \exp\{-\alpha \eta F/RT\}$

$|\eta| < 0.01 \text{ V}$ Charge transfer resistance

$i = 2i_0 \sin(F\eta/2RT) \approx 2i_0 (F\eta/2RT) = i_0 (F\eta/RT)$

For $\eta \approx 0.01 \text{ V} - 0.1 \text{ V}$

=> Use the BV-equation. The BV equation can be used as is for any case.

Exercise 1

Calculate the ratio of the rates of the reaction: $\text{Ag}^+ + \text{e}^- \rightarrow \text{Ag}$ at:

a) $\eta = -0.15 \text{ V}$ & $\eta = 0.15 \text{ V}$.

b) $\eta = -0.2 \text{ V}$ & $\eta = 0.2 \text{ V}$.

Assume room temperature at 25°C .

Exercise 2

For an overpotential of $\eta = 10 \text{ mV}$, a current $I = 0.62 \text{ mA}$ is passed through a 2 cm^2 Pt electrode for a H^+/H_2 half reaction given as: $\text{H}^+ + \text{e}^- \rightarrow \frac{1}{2} \text{H}_2$.

What will be the current density i for (a) $\eta = 100 \text{ mV}$? (b) $\eta = -100 \text{ mV}$?

Assume the symmetry factor as 0.5 and a room temperature of 25°C

Exercise 3

The exchange current density of a Pt electrode for the H^+/H_2 half reaction is $i_0 = 0.79 \text{ mA}\cdot\text{cm}^{-2}$ at 25°C .

Calculate the current density across it when the over potential is (a) $\eta = 10 \text{ mV}$ (b) $\eta = -200 \text{ mV}$.

Exercise 4

Calculate the effective resistance across 1 cm^2 of

- a) Pt, H_2 , H^+ ; $i_0 = 0.79 \text{ mA}\cdot\text{cm}^{-2}$
 b) Hg, H_2 , H^+ ; $i_0 = 0.79 \times 10^{-12} \text{ A}\cdot\text{cm}^{-2}$

What conclusion you can draw from the result?

Exercise 5

In an experiment involving Pt, H_2 , H^+ electrode, the following data were obtained at 298 K. Determine α and i_0

η/mV	50	100	150	200	250
$i / \text{mA}\cdot\text{cm}^{-2}$	3.19	10.69	35.88	120.00	402.00

Exercise 6

For the system Pt / Fe^{3+} , Fe^{2+} at 298K the i were measured as shown below: Determine α and i_0

η/mV	-50	-80	-100	-120	-150	-200
$i / \text{mA}\cdot\text{cm}^{-2}$	-8.01	-16.1	-25.17	-41	-82.4	-264
η/mV	50	80	100	120	150	200
$i / \text{mA}\cdot\text{cm}^{-2}$	5.50	8.78	11.91	16.30	26.00	56.60

Exercise 9

The exchange current density of Pt / Fe^{3+} , Fe^{2+} is $2.5 \text{ mA}\cdot\text{cm}^{-2}$.

Calculate the current density across the electrode at 25°C maintained at 1 V when $[\text{Fe}^{2+}] = 0.1 \text{ M}$ and $[\text{Fe}^{3+}] = 0.2 \text{ M}$

(Standard reduction potential = 0.771 V, $\beta = 0.58$)